

**2 0 1 4**

( May )

**PHYSICS**

( Major )

Course : 601

( **Statistical Mechanics** )

Full Marks : 60

Pass Marks : 24

Time : 3 hours

*The figures in the margin indicate full marks  
for the questions*

1. Choose the correct option : 1×5=5

- (a) "With microscopic variables held fixed, the member of an ensemble are neither created nor destroyed."

The above statement is related to

- (i) micro-canonical ensemble
- (ii) canonical ensemble
- (iii) Liouville's theorem
- (iv) grand canonical ensemble

(b) Gibbs function in terms of partition function ( $Z$ ) is

(i)  $VT - NkT \log Z$

(ii)  $RT - NkT \log Z$

(iii)  $RT - NPT \log Z$

(iv)  $PT - NkT \log Z$

the symbols represent their usual meanings.

(c) Which of the following particles is not a boson?

(i) Photon

(ii) Alpha particle

(iii) Helium

(iv) Electron

(d) Fermions are

(i) indistinguishable and spinless particles

(ii) distinguishable and spin half-particles

(iii) indistinguishable, spin half-particles and obey Pauli's exclusive principle

(iv) indistinguishable, spinless particles but does not obey Pauli's exclusive principle

- (e) White dwarfs are
- (i) last stage of a star having mass below Chandrasekhar limit
  - (ii) last stage of a star having mass above Chandrasekhar limit
  - (iii) previous stage of a black hole
  - (iv) None of the above

2. Explain what you mean by phase space, micro-canonical ensembles and grand canonical ensembles. 2+5=7

3. Discuss Maxwell-Boltzmann distribution law and derive the relation

$$n_i = g_i e^{(-\alpha - \beta E_i)} \quad 7$$

4. What do you mean by partition function? 3

5. Express internal energy of  $N$  particle system in terms of partition function. 6

Or

Derive Boltzmann relation between entropy and probability.

6. (a) Write limitations of Maxwell-Boltzmann statistics. 3

- (b) What are the differences between Maxwell-Boltzmann, Bose-Einstein and Fermi-Dirac statistics? 3
- (c) Write the basic postulates of Bose-Einstein statistics. 4
7. (a) Deduce the Fermi-Dirac distribution laws for fermions. 9

Or

Deduce Fermi-Dirac distribution laws for classical particles.

- (b) Write the condition when Fermi-Dirac distribution and Bose-Einstein statistics reduces to Maxwell-Boltzmann statistics. 3
8. (a) Derive Stefan's law from Bose-Einstein distribution law. 5
- (b) Write short note on any one of the following : 5
- (i) Chandrasekhar limit
  - (ii) White dwarfs
  - (iii) Bose-Einstein condensation

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